

# Building Economic Models of Human Computer Interaction: CHI 2019 Course

Leif Azzopardi<sup>1</sup> and Guido Zuccon<sup>2</sup>

<sup>1</sup> Dept. of Computer and Information Sciences, University of Strathclyde, Glasgow,  
Scotland

`leif.azzopardi@strath.ac.uk`

<sup>2</sup> Information Technology and Electrical Engineering School, University of  
Queensland, Brisbane, Australia

`g.zuccon@uq.edu.au`

**Abstract.** This tutorial aims to explain how economics can be used to model the interaction between users and systems. Economic theory provides an intuitive and natural way to model Human-Computer Interaction which enables the prediction and explanation of user behaviour. A central tenet of the approach is the utility maximisation paradigm where it is assumed that users seek to maximise their profit/benefit subject to budget and other constraints when interacting with a system. By using such models it is possible to reason about user behaviour and make predictions about how changes to the interface or the users interactions will affect performance and behaviour. In this tutorial, we describe and develop several economic models relating to how users search for information. While the examples are specific to Information Seeking and Retrieval, the techniques employed can be applied more generally to other human-computer interaction scenarios. Therefore, the goal of this chapter is to provide an introduction and overview of how to build economic models of human-computer interaction that generate testable hypotheses regarding user behaviour which can be used to guide design and inform experimentation.

An extended and interaction version of this tutorial will be presented at CHI 2019, see <https://ielab.io/tutorials/economic-hci.html> for more details. The intended learning outcomes of this tutorial are:

- Define and describe the different types of conceptual and formal models;
- Explain the rationale for formal models in Human Computer Interaction (HCI);
- Define economic (optimization) models for UX/UI and system design
- Explain and infer the predicted user behavior given economic models;
- Design economic models of HCI in order to generate testable hypotheses regarding user behavior.

The tutorial will be split into four parts:

- **Economic and Optimisation Models:** The first session will focus on providing a grounding in economic theory and optimisation models, and how to draw insights and hypothesizes from the models.
- **Information Foraging Theory:** Economics forms the basis of foraging theory and information foraging theory. In this session we explain foraging theory and how it has been used to explain people’s behaviours as they seek to maximise their rate of gain.
- **Theory to Practice:** The third session will focus on applying these concepts to a number of different examples in the search and recommendation context.
- **Build your own model:** Finally in the last session we focus on developing economic models. Participants invited to bring along their own scenario or context.

We will provide a number of running examples through the day, such as “How many apps should be displayed per screen on a tablet?”, “How do players adapt to changes in clash of clans?”, “Is Spotify too good to pay for?”, etc. These will be used in the final session as example scenarios to build an economic model of the interactions - or participants can bring along their own scenarios to model.

The course notes below provide an overview of some of the detailed examples which will be covered during the third session. Slides and other course material will be made available at: <https://ielab.io/tutorials/economic-hci.html>

## 1 Introduction

When interacting with a system, users need to make numerous choices about what actions to take in order to advance them towards their goals. Each action comes at a cost (e.g. time taken, effort required, cognitive load, financial cost, etc.), and the action may or may not lead to some benefit (e.g. getting closer to completing the task, saving time, saving money, finding out new information, having fun, etc.). Describing Human Computer Interaction (HCI) in this way naturally leads to an economic perspective on designing and developing user interfaces. Economics provides tools to model the costs and benefits of interaction where the focus is on understanding and predicting the behaviour and interaction of economic agents/users within an economy/environment. By developing economic models of interaction, it is possible to make predictions about user behaviour, understand the choices they make and inform design decisions. When interaction is framed as an economic problem, we can examine what actions lead to accruing the most benefit for a given cost or incur the least cost for a given level of benefit, from which it is then possible to determine what is the optimal course of action that a rational user *should* take given the task, interface, context and constraints.

Let’s consider a simple example: your friend has just completed a marathon, and you are curious to know how long it took them to complete the race<sup>3</sup>. You

<sup>3</sup> This example is based on a study conducted in [42], where people were challenged to undertake such a task.

have arrived at the web page showing all the times and names of runners, ordered by time. You consider two options: (i) scrolling through the list, or (ii) using the “*find*” command<sup>4</sup>. The first option would mean scrolling through on average about half the list of names, while the second would require selecting the find command, typing in their name, and then checking through the matches. Unless the list is very small, then the second option is probably going to be less costly (i.e. less comparisons) and more accurate<sup>5</sup>. In this example, it may seem obvious that using the “*find*” option would be preferable in most cases - and indeed it is reasonably trivial to develop a simple model of the costs and benefits to show at what point it is better to use the “*find*” option over the “*scroll*” option, and vice versa. However, even to arrive at such an intuition, we have made a number of modelling assumptions:

1. that the user wants to find their friend’s performance (and that the said friend took part in the marathon),
2. that the user knows and can perform both actions,
3. the currency of the costs/benefit is in time i.e. time spent/saved, and,
4. that the user wants to minimize the amount of time spent completing the task.

Such assumptions provide the basis for a formal model to be developed. The last assumption is common to most economic models. This is because they are a type of “optimization” model [31, 32, 38, 37], which assumes that people attempt to maximise their profit given their budget (costs) or minimize their budget expenditure given some level of profit. The other assumptions serve as constraints which are a result of the environment, the limitations of the person, and/or the simplifications made by the modeller. By engaging such an assumption, the model can be used to consider the trade-offs between different strategies, reason about how users will adapt their behaviour as the costs and benefit change, and make predictions about their behaviour. Consequently, economic models go beyond approaches which just focus solely on cost (e.g. GOMS-KLM[14], Fitt’s Law[19], Hick’s Law[22], etc.), as economic models also consider the benefit and profit that one derives from the interaction. This is an important difference, because not all tasks are cost/time driven where the goal is to reduce the time taken or minimize friction. For example, when should an author stop editing a paper, when should an artist stop photoshopping an image, when should a researcher stop searching for related works? In the above example, the different options have varying degrees of accuracy when employed to find the correct runner’s name and subsequent time. This is because as the number of items in the list increases the chance of missing or skipping over an item also increases, thus decreasing the accuracy. So in this case, there is a trade-off between the speed (minimising time taken to complete the task) and the accuracy (finding

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<sup>4</sup> Note that we have assumed that you are familiar with using the “*find*” command (e.g. *CTRL-f*, *CMD-f*, etc). Of course, not all users are familiar with, or even aware that this option is available.

<sup>5</sup> It is easy to skip over records when browsing through thousands of entries. Indeed, in the study conducted in [42], subjects that scrolled often reported the incorrect time.

the correct time). Also when using the “*find*” option, there is another trade-off between the number of letters entered (typing cost) versus the number of matching names (scanning costs, and thus accuracy). In such tasks, it is clear that understanding the trade-off between the benefits and the costs of different interaction strategies can help predict user behaviour. Economic models can help to draw insights into these trade-offs and understand when one strategy (sequence of actions) is better to perform than another or what strategy to adopt under different circumstances.

In economic models, it is commonly assumed that users are economic agents that are rational in the sense that they attempt to maximize their benefits, and can learn to evolve and adapt their strategies towards the optimal course of interaction. Thus the theory is normative, and gives advice on how a rational user *should* act given their knowledge and experience of the system. Going back to the example above, if a user is not aware of the “*find*” option, then they will be limited in their choices, and so they would select the “*scroll*” option (or, choose not to complete the task, i.e. the “*do nothing*” option). However, when they learn about the existence of the “*find*” option, perhaps through exploratory interactions or from other users, then they can decide between the different strategies. While assuming that users are rational may seem like a rather strong assumption, in the context of search a number of works [6, 39, 44, 45] have shown that users adapt to systems and tend to maximize benefit for a given cost (e.g. subscribe to the utility maximisation paradigm [46]) or minimize cost for a given level of benefit (e.g. subscribe to the principle of least effort [52])<sup>6</sup>. So a user, knowing of the “*find*” option would select it when the list of items is sufficiently long such that employing the find command is likely to reduce the total cost incurred. Once we have a model, we can then test such hypotheses about user behaviour, e.g. given the cost of using the find command, the cost of scanning items, etc. then we may hypothesise that when the length of the list is over say two pages, it is more efficient to use the “*find*” option - and then design an experiment to test if this assertion holds in practice (or not) in order to (in)validate the model.

During the course of this chapter, we will first provide an overview of economic modelling in the context of HCI where we will formalise the example above by developing two models that lead to quantitative predictions regarding which option a user should employ (i.e. “*find*” or “*scroll*”), and, how they should use the “*find*” command, when chosen. Following on from this finding example, we will then consider three further search scenarios related to information seeking and retrieval, where we will develop models of: (i) querying, (ii) assessing and (iii) searching. The first model will be provide insights into query length and how to encourage longer or shorter queries. The next model will provide insights into when to stop assessing items in a ranked list of results and how to design different result pages for different result types. The third model on searching will examine the trade-off between issuing queries and how many documents to

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<sup>6</sup> Note that essentially these optimisations objectives are two sides of the same coin and arrive at the same optimal solution i.e. if the maximum benefit is \$10 for 5 minutes of work, then for a benefit of \$10 the minimum cost is 5 minutes of work.

examine per query during the course of search session. This will lead to a number of insights into where the system can be improved and how users will respond to such changes. While these models are focused on search and search behaviour, similar models could be developed to help describe how people browse products, play games, use messaging, find apps, enter text, and so on. In the next section, we will describe a framework for building economic models of interaction that can be used to build your own models, that inform your designs and guide your experimental research.

## 2 Economic Models

An economic model is an abstraction of reality, that is a simplified description of the phenomena in question, designed to yield hypotheses about behaviour that can be tested [36]. There are two types of economic models: *theoretical* and *empirical*.

**Theoretical models** aim to develop testable hypotheses about how people will behave and assume that people are economic agents that maximise specific objectives subject to constraints (e.g., amount of time available for the task, knowledge of potential actions, etc.). Such models provide qualitative answers to questions such as, how does the cost of querying affect the user's behaviour, if the benefit of query suggestions increases, how will user's adapt?

**Empirical models** aim to evaluate the qualitative predictions of theoretical models and realise the predictions they make into numerical outcomes. For example, consider a news app that provides access to news articles for a small payment, and a theoretical model that says that if the cost of accessing news articles increases, then users will reduce their consumption of such articles. Then an empirical model would seek to quantify by how much consumption will drop given a price increase.

Economic models generally consist of a set of mathematical equations that describe a theory of behaviour [36]. According to Ouliaris [36], the aim of model builders is to include enough detail in the equations so that the model provides useful insights into how a rational user would behave and/or how a system works. The equations, and their structure, reflect the model builder's attempt to represent reality in an abstracted form by making assumptions about the system, the user and the environment. Economic models range in complexity. For example, we may model the demand for news articles as inversely proportional to the cost of the article. The less expensive the news articles, the more that they are demanded according to such model. Models however can be much more complex consisting of non-linear, interconnected differential equations that for example predict the flow and transmission of fake news through a social network [25].

**Building Economic Models** Varian has described how to approach the problem of building a useful economic model [47] (which is similar to other model building approaches [12, 15, 32]). The main steps involved when building economics models are:

1. Describe the problem context,
2. Specify the functional relationships between the interactions and the cost and benefit of those interactions,
3. Solve the model,
4. Use the model to generate hypotheses about behaviours,
5. Compare the predictions with observations in the literature and/or experimental data, and,
6. Refine and revise the theory accordingly, and iterate the procedure.

**Step 1 - Describe the Problem Context:** First off, outline what is known about the problem context, the environment and the interface(s) in which the interaction is occurring. It may also help to illustrate the interface(s), even if hypothetical, that the user population will be using. For example, we may want to consider how facets when added to a shopping interface would affect behaviour, and so draw a faceted search interface from which we can consider different ways in which the user can then interact with it [27]. According to Varian all economic models take a similar form, where we are interested in the behaviour of some economic agents [47]. These agents make choices to advance towards their objective(s). And these choices need to satisfy various constraints based upon the individual, the interface and the environment/context. This leads to asking the following questions:

- who are the people making the choices?
- what are their constraints?
- how do they interact with the interface? and
- what factors/constraints in the environment are likely to affect the interaction?

Let's re-visit the scenario we introduced earlier, where we want to know our friend's performance in the marathon. Imagine, we are at the page containing a list of the names and their race completion times. And let's assume we are tech savvy individuals. We are aware of several choices: (i) search by scrolling, (ii) search via the find command, (iii) some combination of scrolling and finding. To make things simple we consider only the first two and assume that we only select one or the other. We would like to try and find out as quickly as possible our friend's race time because we'd like to see whether we ought to congratulate our friend or sympathise with them. So in this case, the objective is to minimize the time taken to find their name. Since time is at a premium, we have a constraint such that we want to complete the search within a certain period of time (after which we may give up), or, if we believe we could not complete the task within the time constraint, then we may decide not to search at all. In this later case, where we decide not to search, we may take some other action like asking our friend. Though, of course, we would like to keep the initiative in the conversation from which we will derive benefit. In terms of interaction with the page, if we (i) scroll, then we plan to look down the list, one by one, and see if we recognise our friend's name in the list, while if we (ii) use command find, we plan to

type in a few letters of their name, and step through each matching name. In both cases, we also acknowledge that there is some chance of skipping over their name and so there is some probability associated with finding their name - such that as the list of names that has to be checked increases, the chance of missing also increases. We also can imagine that in case (ii) if we enter more letters the list of names to check decreases proportionally with each additional letter. We can now formalise the problem with a series of assumptions (like those listed in Section 1), and then start to model the process mathematically.

**Step 2 - Specify the Cost and Benefit functions:** For a particular strategy/choice, we need to identify and enumerate the most salient interactions which are likely to affect the behaviour when using the given interface. At this point, it is important to model the interaction at an appropriate level - too low and it becomes unwieldy (i.e. modelling every keystroke), too high and it becomes uninformative (i.e. simply considering the aggregated cost/benefit of the scroll option vs. the cost/benefit of find option). Varian [47] suggests to keep this as simple as possible:

*“The whole point of a model is to give a simplified representation of reality...your model should be reduced to just those pieces that are required to make it work”.*

So initially focus on trying to model the simplest course of action, at the high level possible, to get a feel for the problem, and then refine. If we start too high level, we can then consider what variables influence the cost of the scroll option (i.e. the length of the list), and start to parameterise the cost function, etc. We can also reduce the complexity of the interaction space, so, for example, in the facet shopping interface, we might start with one facet, and then progress to two facets. Essentially, make the problem simple and tractable to understand what is going on. The simple model that is developed will probably be a special case or an example. The next important step is to generalize the model, e.g., how do we model  $f$  facets?

In our scenario, for option ( $i$ ) we need to perform two main actions: scroll ( $scr$ ) and check ( $chk$ ), where we will assume that the cost of a scroll is per item ( $\mathbf{c}_{scr}$ ), and the cost of checking the name is also per item ( $\mathbf{c}_{chk}$ ). In the worse case, we'd need to scroll through and check  $\mathbf{N}$  names, while in the average case we'd only need to examine approximately half of the names  $\mathbf{N}/2$ , and in the best case our friend came first, so  $\mathbf{N} = 1$ . Let's consider the average case, where then, the cost of option ( $i$ ) would be:

$$\mathbf{C}_{(i)}(\mathbf{N}) = \frac{\mathbf{N} \cdot (\mathbf{c}_{scr} + \mathbf{c}_{chk})}{2} \quad (1)$$

We also know that the benefit is proportional to our likelihood of success and that is conditioned on how many items we need to check through, so we can let the probability of successfully finding our friend's name be  $\mathbf{p}_{scr}(\mathbf{N})$ . Thus we can formulate an expected benefit function, i.e. the benefit that we would expect to receive on average:

$$\mathbf{B}_{(i)}(\mathbf{N}) = \mathbf{p}_{\text{scr}}(\mathbf{N}) \cdot \mathbf{b} \quad (2)$$

where  $\mathbf{b}$  is the benefit, e.g., the time saved from having to hear your friend going on and on about how you are not interested in them, and how you couldn't even find it on the computer, etc. Now we can create a profit function to denote how much time we expect to save/lose if we take this option. A profit function is the difference between the benefit function and the cost function:

$$\pi_{(i)} = \mathbf{B}_{(i)}(\mathbf{N}) - \mathbf{C}_{(i)}(\mathbf{N}) = \mathbf{p}_{\text{scr}}(\mathbf{N}) \cdot \mathbf{b} - \frac{\mathbf{N}(\mathbf{c}_{\text{scr}} + \mathbf{c}_{\text{chk}})}{2} \quad (3)$$

On the other hand, for option (ii), we need to perform a different sequence of actions: command find (*cmd*), type (*typ*), skip (*skp*) and check (*chk*), where we will assume that the cost to evoke command find is  $\mathbf{c}_{\text{cmd}}$ , to type in a letter is  $\mathbf{c}_{\text{typ}}$  and to skip to the next match is  $\mathbf{c}_{\text{skp}}$ . For simplicity, we will assume the cost of a skip and the cost of a scroll be the same  $\mathbf{c}_{\text{skp}} = \mathbf{c}_{\text{scr}}$ . The course of interaction is press command find, type in  $\mathbf{m}$  letters, and then skip through the results, checking each one. Since typing in  $\mathbf{m}$  letters will reduce the number of checks, we assume that there is a function  $\mathbf{f}(\mathbf{N}, \mathbf{m})$ , which results in a list of  $\mathbf{M}$  to check through (and as  $\mathbf{m}$  increases,  $\mathbf{M}$  decreases). Again we are concerned with the average case, if there are  $\mathbf{M}$  matches, then we'd only need to examine approximately half, i.e.  $\mathbf{M}/2$ . Putting this all together, we can formulate the following cost function, which takes in both the size of the list and the number of letters we are willing to enter:

$$\mathbf{C}_{(ii)}(\mathbf{N}, \mathbf{m}) = \mathbf{c}_{\text{cmd}} + \mathbf{m} \cdot \mathbf{c}_{\text{typ}} + \frac{\mathbf{M}(\mathbf{c}_{\text{scr}} + \mathbf{c}_{\text{chk}})}{2} \quad (4)$$

We can also formulate the benefit function, which also takes in  $\mathbf{N}$  and  $\mathbf{m}$  as follows:

$$\mathbf{B}_{(ii)}(\mathbf{N}, \mathbf{m}) = \mathbf{p}_{\text{scr}}(\mathbf{f}(\mathbf{N}, \mathbf{m})) \cdot \mathbf{b} = \mathbf{p}_{\text{scr}}(\mathbf{M}) \cdot \mathbf{b} \quad (5)$$

where, since  $\mathbf{M}$  will be typically much smaller than  $\mathbf{N}$ , the expected benefit will typically be higher. Again we can formulate a profit function  $\pi_{(ii)}$  by taking the difference between the benefit and cost function.

**Step 3 - Solve the model:** The next step is to solve / instantiate the model in order to see what insights it reveals about the problem being studied. This can be achieved through various means: analytically, computationally or graphically. For example, we could determine which option would be more profitable,  $\pi_{(i)}$  or  $\pi_{(ii)}$ , by taking the difference and seeing under what circumstances option (i) is better than (ii), and vice versa. We could achieve this analytically, i.e. if  $\pi_{(i)} > \pi_{(ii)}$ , then select option (i), else (ii). Alternatively, we could instantiate the model, with a range of values, and plot the profit functions of each to see when  $\pi_{(i)} > \pi_{(ii)}$ , and under what conditions. Or in the case of option (ii), we could consider the tradeoff between typing more letters and the total time to find the name - and find the optimal number of letters to type. Note, above we have not specified the form of the functions  $\mathbf{f}(\mathbf{N}, \mathbf{m})$  or  $\mathbf{p}_{\text{scr}}(\cdot)$ ; so in order



to solve or plot, we would need to make some further assumptions, or look to empirical data for estimating functional forms.

So if we are interested in deciding which option to take, then we can try and solve the inequality  $\pi_{(i)} > \pi_{(ii)}$ , which we can reduce to:

$$\mathbf{c}_{\text{cmd}} + \mathbf{m} \cdot \mathbf{c}_{\text{typ}} > (\mathbf{N} - \mathbf{M}) \cdot (\mathbf{c}_{\text{scr}} + \mathbf{c}_{\text{chk}}) \quad (6)$$

where we have assumed that  $\mathbf{p}(\mathbf{N})$  is approximately equal to  $\mathbf{p}(\mathbf{M})$  for the sake of simplicity i.e. we are assuming that the two methods perform the same (even though this is probably not the case in reality). To plot the model graphically, we further assumed that,  $\mathbf{f}(\mathbf{N}, \mathbf{m}) = \frac{\mathbf{N}}{(\mathbf{m}+1)^2}$ , to reflect the intuition that more letters entered will reduce the number of names to check. Later we could also empirically estimate the form based on a computational simulation, i.e. given a list of names, we could count how many names are returned, on average, when  $\mathbf{N}$  and  $\mathbf{m}$  are varied in order to gather actual data to fit a function. Next we have to provide some estimates of the different costs. Here, we have set  $\mathbf{c}_{\text{typ}}$  to be 1 second per letter,  $\mathbf{c}_{\text{cmd}}$  to be 15 seconds,  $\mathbf{c}_{\text{scr}}$  and  $\mathbf{c}_{\text{skp}}$  to be 0.1 seconds per scroll/skip and  $\mathbf{c}_{\text{chk}}$  to be 0.5 seconds per name check. Of course, these values are only loosely based on the time taken to perform such actions. To create a more precise instantiation of the model, we would need to empirically ground these values. Part of the model building process involves iteratively refining the parameters and their estimates based on observed data. But, initially, we can get a “*feel*” for the model by using some reasonable approximations. Figure 1 shows a plot of the inequality when  $\mathbf{m} = 2$  (top) and  $\mathbf{m} = 7$  (bottom).

Now, focusing on option (ii), we can calculate the optimal way to interact when using the find command, i.e. how many letters should we type? To do this, we can consider maximising the profit with respect to the number of letters we need to type (as this reduces the number of possible matches to skip through). To achieve this, we instantiate the profit function for option (ii), where we assume, for simplicity, that  $\mathbf{p}_{\text{scr}}(\mathbf{M}) = 1$ , such that:

$$\pi_{(ii)} = \mathbf{b} - \left( \mathbf{c}_{\text{cmd}} + \mathbf{m} \cdot \mathbf{c}_{\text{typ}} + \frac{\mathbf{N}}{2 \cdot (\mathbf{m} + 1)^2} (\mathbf{c}_{\text{scr}} + \mathbf{c}_{\text{chk}}) \right) \quad (7)$$

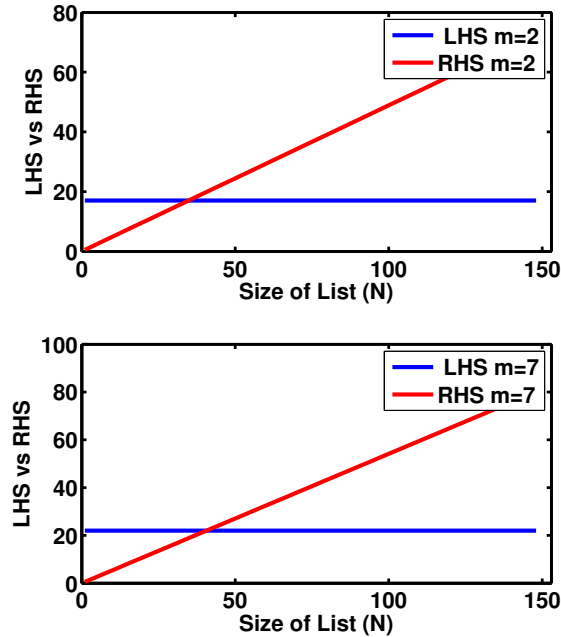
then we can differentiate the profit function with respect to  $\mathbf{m}$  to arrive at:

$$\frac{d\pi_{(ii)}}{d\mathbf{m}} = -\mathbf{c}_{\text{typ}} + \mathbf{N} \cdot (\mathbf{c}_{\text{scr}} + \mathbf{c}_{\text{chk}}) \cdot (\mathbf{m} + 1)^{-3} \quad (8)$$

Setting  $\frac{d\pi_{(ii)}}{d\mathbf{m}} = 0$ , we obtain the following expression for  $\mathbf{m}^*$ , which is the optimal number of letters to enter for a list size of  $\mathbf{N}$ :

$$\mathbf{m}^* = \left( \frac{\mathbf{N} \cdot (\mathbf{c}_{\text{scr}} + \mathbf{c}_{\text{chk}})}{\mathbf{c}_{\text{typ}}} \right)^{\frac{1}{3}} - 1 \quad (9)$$

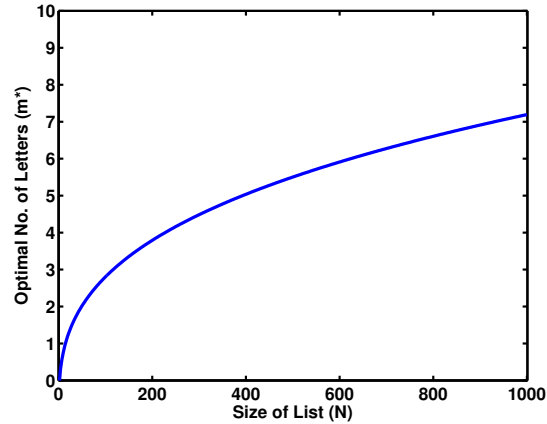
Figure 2 shows a plot of the optimal number of letters ( $\mathbf{m}^*$ ) as  $\mathbf{N}$  increases. As expected, more letters are required as  $\mathbf{N}$  increases, but at a diminishing rate.



**Fig. 1.** Top: Plot of the inequality when only 2 letters are entered, Bottom: Plot of the inequality when 7 letters are entered, where if  $LHS > RHS$  then scroll, else use the find command. The plots suggest that once the size of the list is greater than 30-40 items, using the find command is less costly. But as  $m$  increases, a longer list is required to justify the additional typing cost.

**Step 4 - Use the model and hypothesise about interaction:** Given the models created above, we can now consider: how different variables will influence interaction and behaviour, find out what the model tells us about optimal behaviour, and see what hypotheses can be generated from the model.

From Eq 6 and Figure 1, we can see that if the cost of using the find command is very high, then the list will have to be longer before it becomes a viable option. There is a trade-off between the number of letters entered ( $m$ ) and the reduction in  $M$ , which is of course proportional to  $m$ . From the plots, we can see that moving from  $m = 2$  to  $m = 7$  does not have a dramatic impact on when we'd decide to scroll or find. However, a longer list is needed to warrant the entry of more letters. Furthermore, from the graphs, we can see that, in these examples, once the list contains more than 40-50 names, it is better to use the find command. Exactly, where this point is, depends on how we estimate the various costs and instantiate the functions used. However, it is possible to create hypotheses about how people would change their behaviour in response to different circumstances. For example, we could imagine a similar scenario where



**Fig. 2.** Top: Plot of  $m^*$  versus the size of the result list ( $N$ ).

the cost of comparison is very high, because we are trying to match a long unique number that represents each runner instead (and so hypothesise that using the find command is preferable when lists are even shorter).

From Eq. 9 and Figure 2, we can see that as the list size increases the optimal number of letters to enter (given our model) increases, such that 4 letters are optimal when the list is around 250 in size, while around 7 letters are required when the list grows to 1000. Given these estimates, we can then hypothesise that for large lists (around 1000 in size), users will tend to enter, on average, 7 letters, while for shorter lists (around 200-300), users will tend to enter, on average, 4 letters.

**Step 5 - Compare with observed behaviour:** The next step is to determine whether the hypothesis made using the model are consistent with with empirical observations from the literature, and/or to validate the model by designing empirical experiments that explicitly test the hypotheses.

This is an important step in the process for two reasons: (a) the model provides a guide for what variables and factors are likely to influence the behaviour of users, and thus enables us to inform our experiments, and (b) it provides evidence which (in)validates the models, which we can use to refine our models. From the experimental data, we may discover that, for instance, users performed in a variety of ways we did not consider or that we ignored. For example, maybe a significant proportion of users adopted a mixed approach, scrolling a bit first, then using the find command. Or when they used the find command, they misspelt the name or couldn't remember the exact spelling, and so there is some probability associated with entering in the correct partial string to match the name. As a consequence, we find that the model, or the estimates, need to be refined, and so the final step (6) is to iterate: refining and revising the model and it's parameters accordingly. Once we have conducted an empirical investigation,

we can better estimate the costs and benefits. Alternatively, they allow us to develop new models to cater for different interactions and conditions. With this respect, Box notes that:

*“All models are wrong but some are useful”*. [12]

He points out that it would be remarkable if a simple model could exactly represent a real world phenomena. Consequently, he argues that we should build parsimonious models because model elaboration is often not practical, but adds increased complexity, without necessarily improving the precision of the model (i.e. how well the model predicts/explains the phenomena). This is not to say that we should be only building very simple models; instead, Box [12] argues we should start simple, and then only add the necessary refinements based on our observations and data, to generate the next tentative model, which is then again iterated and refined, where the process is continued depending on how useful further revisions are judged to be. That is, there is a trade-off between the abstraction of the model and the predictions that it makes - the less abstracted, the greater the complexity, with perhaps increased model precision. Therefore, the refinements to the model can be evaluated by how much more predictive or explanatory power the model provides about the phenomena.

Following this approach helps to structure how we develop models, and crucially how we explain them to others and use the models in practice. The approach we have described here is similar to the methodology adopted when applying the Rational Analysis method [2, 15], which is a more general approach that is underpinned by similar assumptions. However, here we are concerned with building economic models as opposed to other types of formal models e.g. [38, 32, 37, 31]. During the remaining of the chapter, we shall describe three different, but related economic models of human-computer interaction, where a user interacts with a search engine. Our focus is on showing how theoretical economics models can be constructed (i.e. steps 1-4) and discuss how they provide insights into observed behaviours and designs.

### 3 An Economic Model of Querying

We first consider the process of a user querying a search engine. The model that we will develop will focus on the relationship between the length of the query and the costs/benefits of the query given its length. This is because a user directly controls how long their query is, and query length is strongly related to performance [24], as short queries tends to be vague, while a long queries tends to be more specific. Of course, other factors also influence the performance of a query, i.e. the choice of terms, the type of search task, etc. For simplicity, however, we will only focus on length, as the primary factor affecting performance and behaviour. Using the model we wish to answer the following questions.

- what is the trade-off between cost and benefit over length?
- what is the optimal length of a query?

– how does the length of a query change when the costs/benefits change?

**Problem Context:** Before answering these questions, let’s first consider what we know about the length of queries, and how query length relates to performance. Typically, user queries tend to be short: in a typical web search scenario they have been measured to be around two to three terms in length [3]. On the other hand, it has been shown on numerous occasions that longer queries tend to yield better performance [4, 11, 17], but as queries get longer the performance increases at a diminishing rate [4]. This has led designers and researchers to develop interfaces that try to elicit longer queries from the user [1, 23, 29, 30]. For example, in [1], they used a halo effect around the query box, such that as the user types a longer query the halo changes from a red glow to a blue glow. However, these attempts have largely been ineffectual and have not been replicated outside the lab [23]. So can the model provide insights into why this is the case, why user queries tend to be short, and how we could improve the system to encourage longer queries?

**Model:** To create an economic model of querying, we need to model the benefit associated with querying and model the cost associated with querying. Let’s assume that the user enters a query of length  $\mathbf{W}$  (the number of words in the query). The benefit that a user receives is given by the benefit function  $\mathbf{b}(\mathbf{W})$  and the cost (or effort in querying) defined by the cost function  $\mathbf{c}(\mathbf{W})$ . Here we make a simplifying assumption: that cost and benefit are only a function of query length.

Now let’s consider a benefit function which denotes the situation where the user experiences diminishing returns such that as the query length increases they receive less and less benefit (as shown by Azzopardi [4] and Belkin et al. [11]). This can be modeled with the function:

$$\mathbf{b}(\mathbf{W}) = \mathbf{k} \cdot \log_{\mathbf{a}}(\mathbf{W} + 1) \quad (10)$$

where  $k$  represents a scaling factor (for example to account for the quality of the search technology), and  $\mathbf{a}$  influences how quickly the user experiences diminishing returns. That is as  $\mathbf{a}$  increases, additional terms contribute less and less to the total benefit, and so the user will experience diminishing returns sooner.

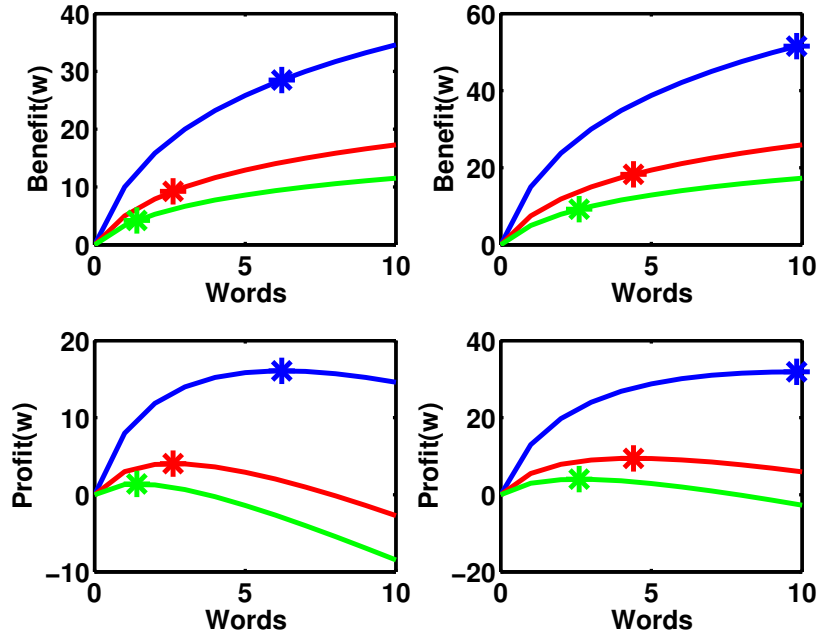
Next, let’s assume that the cost of entering a query is a linear function based on the number of words such that:

$$\mathbf{c}(\mathbf{W}) = \mathbf{W} \cdot \mathbf{c}_w \quad (11)$$

where  $c_w$  represents how much effort must be spent to enter each word. This is, of course, a simple cost model and it is easy to imagine more complex cost functions. However the point is to provide a simple, but insightful, abstraction.

**Optimal Querying Behaviour:** Given the cost and benefit functions, we can compute the profit (net benefit)  $\pi$  that the user receives for a query of length  $W$ :

$$\pi = \mathbf{b}(\mathbf{W}) - \mathbf{c}(\mathbf{W}) = \mathbf{k} \cdot \log_{\mathbf{a}}(\mathbf{W} + 1) - \mathbf{W} \cdot \mathbf{c}_w \quad (12)$$



**Fig. 3.** The top plots show the benefit while the bottom plots show the profit as the length of the query increases. Plots on the right show when the queries yield greater benefit (left  $k = 10$ ; right  $k = 15$ ). Each plot shows three levels of  $\mathbf{a}$  which denotes how quickly diminishing returns sets in.

To find the query length that maximizes the user's net benefit, we can differentiate with respect to  $W$  and solve the equation:

$$\frac{\partial \pi}{\partial W} = \frac{k}{\log \mathbf{a}} \cdot \frac{1}{W+1} - c_w = 0 \quad (13)$$

This results in:

$$W^* = \frac{k}{c_w \cdot \log \mathbf{a}} - 1 \quad (14)$$

**Hypotheses:** Figure 3 illustrates the benefit (top) and profit (bottom) as query length increases. For the left plots  $k = 10$ , and for the right plots  $k = 15$ . Within each plot we show various levels of  $\mathbf{a}$ . These plots show that as  $k$  increases (i.e. overall the performance of the system increases), the model suggests that query length, on average, would increase. If  $\mathbf{a}$  increases (i.e. additional terms contribute less and less to the overall benefit), then queries decrease in length. Furthermore the model suggests that as the cost of entering a word,  $c_w$ , decreases then users will tend to pose longer queries.

**Discussion:** This economic model of querying suggests that to motivate longer queries either the cost of querying needs to decrease or the performance of the system needs to increase (either by increasing  $\mathbf{k}$  or decreasing  $\mathbf{a}$ ). The model provides several testable hypotheses, which provide key insights that inform the design of querying mechanisms and help explain various attempts to encourage longer queries. For example, the query halo does not reduce cost, nor increase benefit, and so is not likely to change user behaviour [23]. On the other hand, the inline query auto-completion functionality now provided by most search engines, reduces the cost of entering queries (e.g., less typing to enter each query term), and also increases the quality of queries (e.g., fewer mis-spellings, less out of vocabulary words, etc. ). Thus according to the model, since the key drivers are affected, queries are likely to be longer when using query auto-completion than without.

While this model provides some insights into the querying process and the trade-off between performance and length, it is relatively crude. We could model more precisely the relationship between the number of characters, number of terms and the discriminative power of those terms, and how they influence performance. Furthermore, depending on the search engine, the length of a query relative to performance will vary, and may even decrease as length increases. For instance, if our search engine employed an implicit Boolean “AND” between terms, then as the number of query terms increases the number of results returned decreases - and so fewer and fewer relevant items are returned (if any). In this case, we would need to employ a different benefit function to reflect and capture this relationship. It is only when we empirically explore, either through an analysis of query logs [23], user judgements and ratings [48], or computational simulations [4, 5] that we can test and refine the model, updating the assumptions and cost/benefit functions/parameters.

## 4 A Model of Assessing

In this section, we consider how people interact with a list of search results after they pose a query to a search engine. Intuitively, when examining search results a person decides to stop at some point in the ranked list and either stop searching altogether, being satisfied with what they have found (or not), or decides to issue a new query and continue searching. Here we will only consider a person’s interaction with one list of results. From the literature, a number of studies have been conducted examining the question of when users decide to stop. The general finding is that users stop when they have found “*enough*” [18, 40, 50]. Other research has suggested that people employ stopping rules, such as, stop after  $n$  non-relevant results [16] or stop when the results do not provide any new information [13]. While these rules are reasonably intuitive, perhaps we can be more formal by modelling the process and considering the following questions:

- what is the trade-off between benefit over assessment depth?
- what is the optimal stopping point?

- how does the depth change in response to changes in costs and benefits?

**Problem Context:** Let’s consider the interaction with the search engine. After a user poses a query, most search engines return a list of results, typically ranked in decreasing likelihood of being relevant to the user’s query [41]. This implies that as the user goes down through the ranked list the benefit that they receive (or the expected benefit) decreases – and so at some point the cost outweighs the benefit of assessing a subsequent item. Of course, there are lots of factors that affect when people stop. For example, if a user types in a “*dud*” query, which retrieves no relevant items, they are likely to stop after only examining a few items, if any. If the user enters “*good*” query, which retrieves many relevant items, then when they stop is probably more task or time dependent. If a user wants to find many relevant items, they presumably they would go deeper. But of course they don’t want to waste their time assessing non-relevant items and so will stop at some point, or if they find enough then they will stop. On the other hand, if they only want one relevant item, then they will stop once they find one item. So the model we develop will need to be sensitive to these different conditions.

**Model:** To create an economic model of assessing, we need to formulate cost and benefit functions associated with the process. Let’s start off by modelling the costs. A user first poses a query to the search engine and thus incurs a query cost  $\mathbf{c}_q$ . Then for the purposes of the model, we will assume the user assesses items, one by one, where the cost to assess each item is  $\mathbf{c}_a$ . If the user assesses  $\mathbf{A}$  items, then the cost function would be:

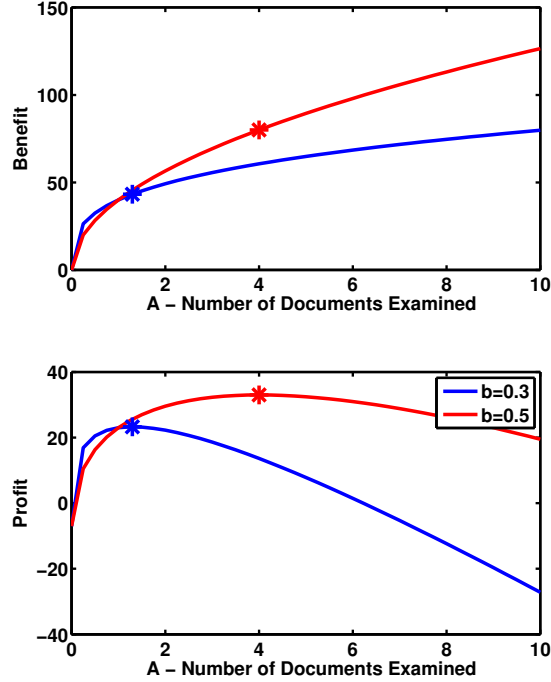
$$\mathbf{c}(\mathbf{A}) = \mathbf{c}_q + \mathbf{A} \cdot \mathbf{c}_a \quad (15)$$

Now, we need a function to model the benefit associated with assessing  $\mathbf{A}$  items. Consider the scenario where a user is searching for news articles, and that they are reading about the latest world disaster. The first article that they read provides key information, e.g. that an earthquake has hit. The subsequent articles start to fill in the details, while others provide context and background. As they continue to read more and more news articles the amount of new information becomes less and less as the same “*facts*” are repeated. Essentially, as they work their way down the ranked list of results, they experience diminishing returns. That is, each additional item contributes less and less benefit. So we can model the benefit one receives as follows:

$$\mathbf{b}(\mathbf{A}) = \mathbf{k} \cdot \mathbf{A}^\beta \quad (16)$$

where  $\mathbf{k}$  is a scaling factor, and  $\beta$  represents how quickly the benefit from the information diminishes. If  $\beta$  is equal to one, then for each subsequent item examined, the user receives the same amount of benefit. However if  $\beta$  is less than one, then for each subsequent item examined, the user receives less additional benefit. This function is fairly flexible: if  $\mathbf{k} = \mathbf{0}$  for a given query, then it can represent a “*dud*” query, while  $\beta = \mathbf{0}$  models when only one item is of benefit (e.g.  $\mathbf{A}^{\mathbf{0}} = \mathbf{1}$ ). So the benefit function can cater for a number of different scenarios.





**Fig. 4.** Top: Plot of the benefit of assessing, Bottom: Plot of the profit of assessing where the result list is of low quality ( $\mathbf{b} = \mathbf{0.3}$ ) and higher quality ( $\mathbf{b} = \mathbf{0.5}$ ). The model predicts users will assess more documents as the result list quality increases.

**Optimal Assessing Behaviour:** Now given these two functions, we can compute the profit (i.e., net benefit)  $\pi$  that the user receives when they assess to a depth of  $\mathbf{A}$ :

$$\pi = \mathbf{b}(\mathbf{W}) - \mathbf{c}(\mathbf{W}) = \mathbf{k} \cdot \mathbf{A}^\beta - \mathbf{c}_q - \mathbf{A} \cdot \mathbf{c}_a \quad (17)$$

To find the assessment depth that maximizes the user's net benefit, we can differentiate with respect to  $\mathbf{A}$  and solve the equation:

$$\frac{\partial \pi}{\partial \mathbf{A}} = \mathbf{k} \cdot \beta \cdot \mathbf{A}^{\beta-1} - \mathbf{c}_a = 0 \quad (18)$$

This results in:

$$\mathbf{A}^* = \left( \frac{\mathbf{c}_a}{\mathbf{k} \cdot \beta} \right)^{\frac{1}{\beta-1}} \quad (19)$$

**Hypotheses:** From Equation 19, we can see that the optimal depth is dependent on the cost of assessment ( $\mathbf{c}_a$ ), and the performance surmised by  $\mathbf{k}$  and

$\beta$ . Using comparative statics [46], we can see how a user should respond when one variable changes, and everything else is held constant. If the cost of assessing increases, and  $\beta$  is less than one (i.e. diminishing returns), then the model suggests that the user would examine less documents. For example, consider a news app that charges per article, while another does not. In this case, the model predicts that users would read less documents in the first app, when compared to the second.

Figure 4 shows how the profit of assessing changes as the cost of assessing is increased. If the performance increases, i.e.  $\beta$  tends to one, then the user would examine more documents. Similarly, as the performance increases via  $\mathbf{k}$ , then this also suggests that the user would examine more documents.

**Discussion:** Intuitively, the model makes sense: if the performance of the query was very poor, there is little incentive/reason to examine results in the list. And if the cost of assessing documents is very high, then it constrains how many documents are examined. For example, consider the case of a user searching on their mobile phone when the internet connection is very slow. The cost of visiting each page is high (i.e. it takes a lot of time to download the page, and may not even load properly), so the model predicts that users are less likely to click and assess documents. Alternatively, consider the case of a user searching for images. The cost of assessing thumbnails (and thus the image) is very low (compared to examining text snippets), and so the model predicts that a user will assess lots of images (but few text snippets). Interestingly, under this model, the cost of a query does not impact on user behaviour. This is because it is a fixed cost, and the analysis is only concerned with the change in cost versus the change in benefit (i.e. stop when the marginal cost equals the marginal benefit). However, in reality the cost of the query is likely to influence how a user behaves. Also, users are likely to issue multiple queries, either new queries or better reformulations which lead to different benefits. While this simple model of assessing provides some insights into the process, it is limited, and may not generalise to these other cases<sup>7</sup>. Next, we extend this model and consider when multiple queries can be issued, and how the trade-off between querying and assessing affects behaviour.

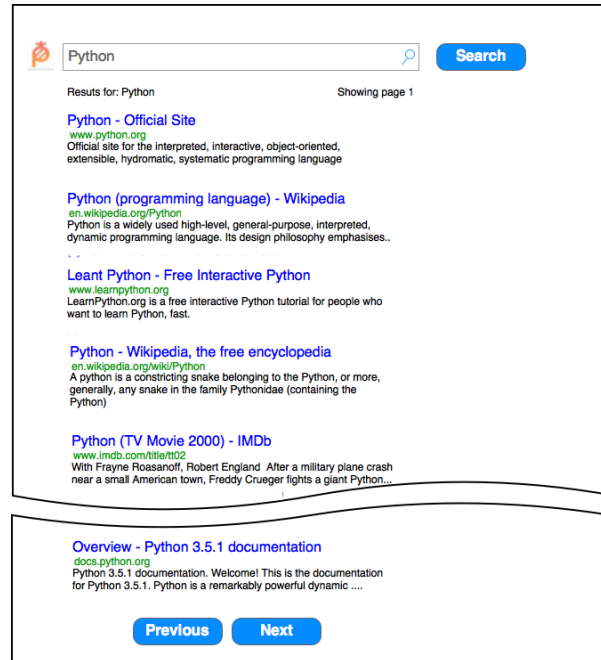
## 5 A Model of Searching

This section describes the process of searching over a session, where numerous queries can be issued, and the user examines a number of items per query. The model will focus on the different search strategies that users can undertake and how the costs and benefits affect the optimal search strategy; specifically, we will explore the following questions:

- what is the trade-off between querying and assessing?
- what is the optimal search strategy?

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<sup>7</sup> As an exercise the reader may wish to consider a model where two queries are issued, and the benefit function is different between queries. See Azzopardi and Zuccon [8] for a solution.



**Fig. 5.** Standard Search Interface – showing results for the query “python”.

- how does the search strategy change in response to changes in costs and benefits?

Essentially, given a particular context, we would like to know if a user should issue more queries and assess fewer items per query, or whether they should issue fewer queries and assess many items per query?

**Problem Context:** Let’s first consider the standard search interface (much like a web search interface) consisting of a query box (or query area) and search button. When a user issues a query to the search engine, the search result page is shown and displays: (i) the number of search results, (ii) the current page number, (iii) a list of  $n$  result snippets (usually  $n = 10$  result snippets per page) and (iv) a next and previous button, see Figure 5. Each search result has a title (often shown as a blue link), a snippet from the item, along with the URL/domain. This style of interface is usually referred to as the “*ten blue links*” [28].

Given this interface, the user can perform a number of actions: (i) (re)query, (ii) examine the search results page, (iii) inspect individual result snippets, (iv) assess items, e.g., click on the result and view the web page, image, news article, etc., and (v) visit subsequent results pages. Each of these actions have an associated cost and so are likely to affect search behaviour.

**Model:** Described more formally, during the course of a search session, a user will pose a number of queries ( $Q$ ), examine a number of search result pages

per query ( $\mathbf{V}$ ), inspect a number of snippets per query ( $\mathbf{S}$ ) and assess a number of items per query ( $\mathbf{A}$ ). Each interaction has an associated cost where  $\mathbf{c}_q$  is the cost of a query,  $\mathbf{c}_v$  is the cost of viewing a page,  $\mathbf{c}_s$  is the cost of inspecting a snippet, and  $\mathbf{c}_a$  is the cost of assessing an item. With this depiction of the search interface we can construct a cost function that includes these variables and costs, such that the total cost of interaction is:

$$c(\mathbf{Q}, \mathbf{V}, \mathbf{S}, \mathbf{A}) = \mathbf{c}_q \cdot \mathbf{Q} + \mathbf{c}_v \cdot \mathbf{V} \cdot \mathbf{Q} + \mathbf{c}_s \cdot \mathbf{S} \cdot \mathbf{Q} + \mathbf{c}_a \cdot \mathbf{A} \cdot \mathbf{Q} \quad (20)$$

This cost function provides a reasonably rich representation of the costs incurred during the course of interaction. In modelling the interaction, we have assumed that the number of pages, snippets and items viewed is per query. Of course, in reality, the user will vary the number of pages, snippets and items viewed for each individual query (see Azzopardi and Zucco [8] for how this can be modelled). So,  $\mathbf{V}$ ,  $\mathbf{S}$  and  $\mathbf{A}$  can be thought of as the average number of pages, snippets and items viewed, respectively. Thus, we are modelling how behaviour with respect to these actions changes, on average. Nonetheless, the cost function is quite complex, so we will need to simplify the cost function. To do so, we will need to make a number of further assumptions.

First, we shall ignore the pagination and assume that all the results are all on one page, i.e.  $\mathbf{V} = 1$ . Thus a user does not need to go to subsequent pages (i.e. infinite scroll)<sup>8</sup>. The assumption is quite reasonable as in most cases users only visit the first page of results anyway [7, 28].

Second, we shall assume that the number of items assessed is proportional to the number of snippets viewed, i.e. that users need to first inspect the result snippet, before clicking on and examining an item, thus  $\mathbf{S} \geq \mathbf{A}$ . Furthermore, we can associate a probability to a user clicking on a result snippet,  $\mathbf{p}_a$ , and examining the item. The expected number of assessments viewed per query would then be  $\mathbf{A} = \mathbf{S} \cdot \mathbf{p}_a$ . Substituting these values into the cost model, we obtained:

$$c(\mathbf{Q}, \mathbf{V}, \mathbf{S}, \mathbf{A}) = \mathbf{c}_q \cdot \mathbf{Q} + \mathbf{c}_v \cdot \mathbf{Q} + \mathbf{c}_s \cdot \frac{\mathbf{A}}{\mathbf{p}_a} \cdot \mathbf{Q} + \mathbf{c}_a \cdot \mathbf{A} \cdot \mathbf{Q} \quad (21)$$

We can now reduce the cost function to be dependent only on  $\mathbf{A}$  and  $\mathbf{Q}$ , such that:

$$c(\mathbf{Q}, \mathbf{A}) = (\mathbf{c}_q + \mathbf{c}_v) \cdot \mathbf{Q} + \left( \frac{\mathbf{c}_s}{\mathbf{p}_a} + \mathbf{c}_a \right) \cdot \mathbf{A} \cdot \mathbf{Q} \quad (22)$$

Let's turn our attention to building the benefit function and characterising how much benefit the user receives from their interactions. Given the two main interactions querying and assessing, we assume, as in the previous model, that as a user examines items, they obtain some benefit, but as they progress through the list of items, the benefit they experience is at a diminishing returns. As previously mentioned, when searching for news about the latest crisis, as subsequent news

<sup>8</sup> However, it would be possible to encode the number of page views per query more precisely by using a step function based on the number of snippets viewed, representing the fixed cost incurred to load and view each page of results. The step function would be such that the number of pages viewed  $\mathbf{V}$  would be equal to the number of snippets viewed divided by the number of snippets shown per page ( $\mathbf{n}$ ), rounded up to the nearest integer, i.e.  $\lceil \frac{\mathbf{S}}{\mathbf{n}} \rceil$ .

articles are read, they become less beneficial because they begin to repeat the same information contained in previous articles. In this case, to find out about other aspects of the topic, another related but different query needs to be issued. Essentially, each query issued contributes to the overall benefit, but again at a diminishing returns, because as more and more aspects of the topic are explored, less new information about the topic remains to be found. To characterise this, we shall model the benefit function using the Cobbs-Douglas function [46]:

$$\mathbf{b}(\mathbf{Q}, \mathbf{A}) = \mathbf{k} \cdot \mathbf{Q}^\alpha \cdot \mathbf{A}^\beta \quad (23)$$

where  $\alpha$  represents returns from querying, while  $\beta$  represents the returns from assessing, and  $\mathbf{k}$  is a scaling factor<sup>9</sup>. Let's consider two scenarios when  $\alpha = 0$  and when  $\alpha = 1$ . In the first case, regardless of how many queries are issued  $\mathbf{Q}^0 = \mathbf{1}$ , so issuing more than one query, would be a waste as it would not result in more benefit. In the latter case,  $\mathbf{Q}^1 = \mathbf{Q}$ , there is no diminishing returns for subsequent queries. This might model the case where the user poses independent queries, i.e. the user searches for different topics within the same session, poses queries that retrieve different items for the same topic, or when there is an seemingly endless supply of beneficial/relevant items e.g., procrastinating watching online videos. Given the form in Eq. 23 the benefit function is sufficiently flexible to cater for a wider range of scenarios. In [5], Azzopardi showed this benefit function to fit well with empirical search performance of querying and assessing.

**Optimal Search Behaviour:** Using the model of searching it is now possible to determine what the optimal search behaviour, in terms of  $\mathbf{Q}$  and  $\mathbf{A}$ , would be given the parameters of the model. To do this we assume that the objective of the user is to minimise the cost for a given level of benefit (or alternatively, maximise their benefit for a given cost). This occurs when the marginal benefit equals the marginal cost. We can solve this optimisation problem with the following objective function (using a Lagrangian Multiplier  $\lambda$ ):

$$\Delta = (\mathbf{c}_q + \mathbf{c}_v \cdot \mathbf{v}) \cdot \mathbf{Q} + \left( \frac{\mathbf{c}_s}{\mathbf{p}_a} + \mathbf{c}_a \right) \cdot \mathbf{A} \cdot \mathbf{Q} - \lambda (\mathbf{k} \cdot \mathbf{Q}^\alpha \cdot \mathbf{A}^\beta - \mathbf{b})$$

where the goal is to minimise the cost subject to the constraint that the amount of benefit is  $\mathbf{b}$ . By taking the partial derivatives, we obtain:

$$\frac{\partial \Delta}{\partial \mathbf{A}} = \left( \frac{\mathbf{c}_s}{\mathbf{p}_a} + \mathbf{c}_a \right) \cdot \mathbf{Q} - \lambda \cdot \mathbf{k} \cdot \beta \cdot \mathbf{Q}^\alpha \cdot \mathbf{A}^{\beta-1} \quad (24)$$

and:

$$\frac{\partial \Delta}{\partial \mathbf{Q}} = \mathbf{c}_q + \mathbf{c}_v \cdot \mathbf{v} + \left( \frac{\mathbf{c}_s}{\mathbf{p}_a} + \mathbf{c}_a \right) \cdot \mathbf{A} - \lambda \cdot \mathbf{k} \cdot \alpha \cdot \mathbf{Q}^{\alpha-1} \cdot \mathbf{A}^\beta \quad (25)$$

Setting these both to zero, and then solving, we obtain the following expressions for the optimal number of assessments per query  $\mathbf{A}^*$ :

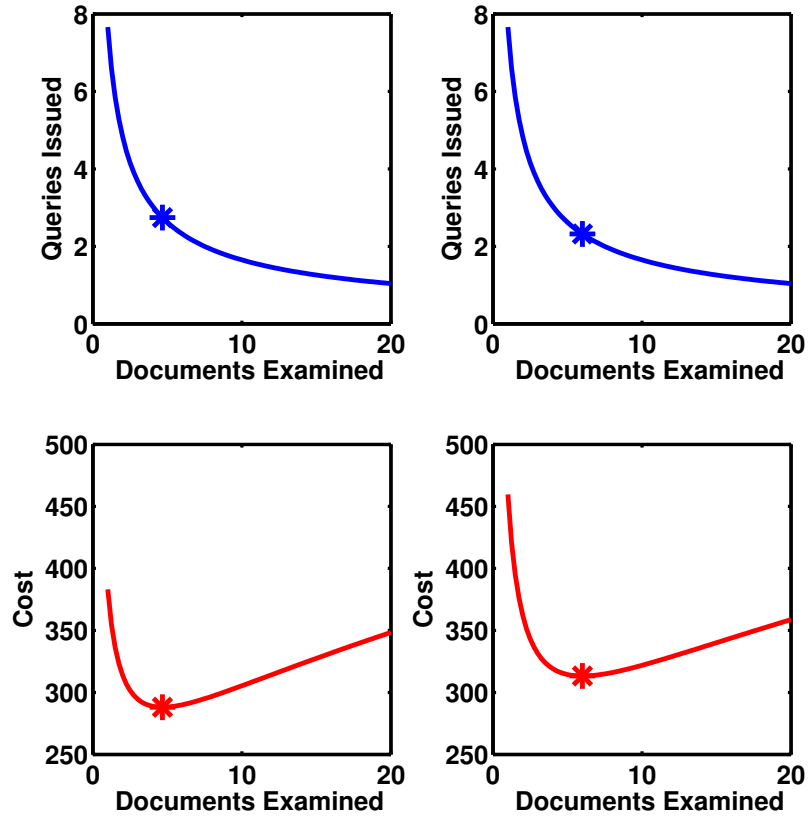
$$\mathbf{A}^* = \frac{\beta \cdot (\mathbf{c}_q + \mathbf{c}_v \cdot \mathbf{v})}{(\alpha - \beta) \cdot \left( \frac{\mathbf{c}_s}{\mathbf{p}_a} + \mathbf{c}_a \right)} \quad (26)$$

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<sup>9</sup> Note that if  $\alpha = 1$  then we arrive at the same benefit as in the model of assessing, see Eq. 16.

and the optimal number of queries  $Q^*$ :

$$Q^* = \sqrt[\alpha]{\frac{g}{k \cdot A^{\beta}}} \quad (27)$$

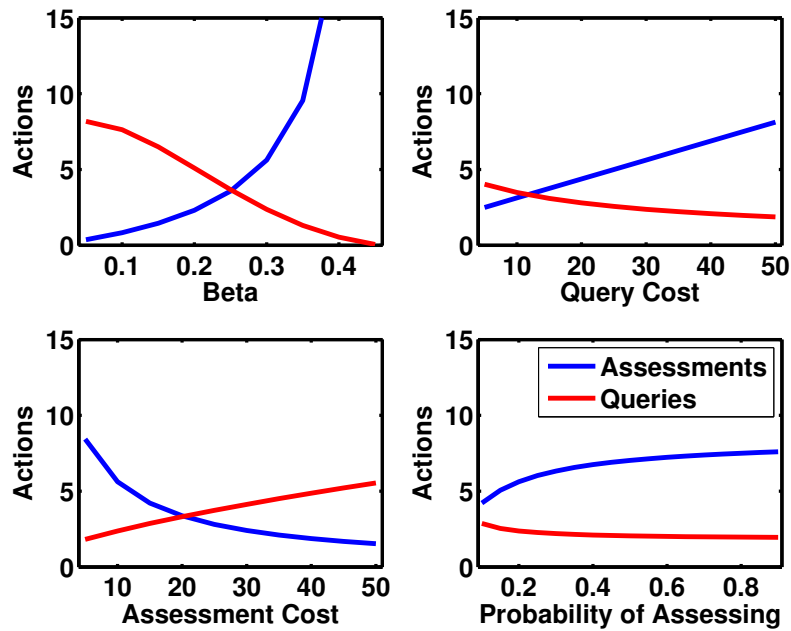


**Fig. 6.** Top: Plots of the number of queries vs. the number of items examined per query for a given level of benefit. Any point yields the same amount of benefit. The asterisk indicates the optimal querying/assessing strategy, i.e.  $(A^*, Q^*)$ . Bottom: Plots of the Cost vs. the number of items examined per query. The asterisk indicates when the cost is minimised, i.e. at  $A^*$ .

**Hypotheses:** Using this analytical solution we can now generate a number of testable hypotheses about search behaviour by considering how interaction will change when specific parameters of the model increase or decrease. From the

model it is possible to derive a number of hypotheses regarding how performance and cost affect behaviour. Rather than enumerate each one below we provide a few examples (see Azzopardi [6] for details on each).

Similar to the previous model, we can formulate a hypothesis regarding the quality of the result list, where as  $\beta$  increases, the number of assessments per query will increase, while the number of queries will decrease (as shown in Figure 7, top left plot). Intuitively, this makes sense because as  $\beta$  increases the rank list of results contains more relevant items: it is better to exploit the current query before switching to a new query.



**Fig. 7.** Top Left: Plot of  $A^*$  and  $Q^*$  as  $\beta$  changes. Top Right: Plot of  $A^*$  and  $Q^*$  as query cost changes. Bottom Left: Plot of  $A^*$  and  $Q^*$  as assessment cost changes. Bottom Right: Plot of  $A^*$  and  $Q^*$  as the probability of assessment changes.

Regarding costs, we can formulate a query cost hypothesis, such that as the cost of a query  $c_q$  increases, the number of items assessed per query will increase, while the number of queries issued will decrease (as shown in Figure 7, top, right plot). It should be clear from the Eq. 26 that this is the case because as  $c_q$  becomes larger,  $A^*$  also becomes larger. In turn, the number of queries issued will decrease, because as  $A^*$  becomes larger,  $Q^*$  tends to zero. Of course, to start the search session, there needs to be at least one query, e.g.,  $Q$  must be equal to one or greater. A similar hypothesis can be formulated regarding

assessment costs, where as the cost of an assessment increases, the number of items assessed per query will decrease, while the number of queries issued will increase. Since the assessment cost  $c_a$  appears in the denominator in Eq. 26 then any increase will reduce the number of assessments.

Another hypothesis that the model produces is regarding the probability of assessing items. Here, as the probability of assessing increases, the number of items assessed increases, while the number of queries issued decreases (as shown in Figure 7, bottom, right plot). If a user examines every item in the ranked list, then  $p_a$  would equal one meaning that for each snippet that they examine, they also examine the item. As a result, because more items are being examined, less queries are issued overall.

**Discussion:** This economic model of searching provides a useful representation of the interaction between a user and a search engine. The model provides a number of insights into different factors that are likely to affect behaviour, and serves as guide on how and where we could improve the system. For example, the search engine could focus on improving the quality of the results, in which case increases in performance should, according to the model, should lead to changes in search behaviour. Or the search engine may want to increase the number of queries, and so may focus on lowering the cost of querying. Of course, the usefulness of the model depends on whether the model hypotheses hold in practice. These hypotheses were tested in two related studies. The first study by Azzopardi et al. [7] explicitly explored the query cost hypothesis where a between groups experiment was devised where the search interface was modified to create different query cost conditions. They used a structured, standard and suggestion based search interface. Their results provided evidence to support the query cost hypothesis, such that when the query cost was high subjects issued fewer queries and examined more items per query, and vice versa. In a follow-up analysis on the same data, the other hypotheses above were explored, and it was shown that they also tend to hold in general [6]. In a study by Ong et al. [33], they conducted a between groups study evaluating the differences in search behaviour when subjects used either a mobile device or a desktop device to perform search tasks. On mobile devices, the costs for querying and assessing are much higher due to smaller keyboard (leading to slower query entry) and bandwidth/latency limitations (leading to slower page downloads). This resulted in subjects assigned to the mobile condition issuing fewer queries, but examining more snippets/items per query [33]. Again, this is broadly consistent with the model developed here.

While the model provides a number of insights into search behaviour for topic based searches, there are a number of limitations and assumptions which could be addressed. For example, the model currently assumes that the user examines a fixed number of snippets/items per query, yet most users examine a variable number of snippets/items per query. Essentially, the model assumes that on average this is how many snippets/items are viewed per query. For a finer grained model, we would have to model each result list individually, so that the total benefit would be, for example, the sum of the benefit obtained from each



result list over all queries issued. Then it would be possible to determine, given a number of queries, how far the user should go into each result list (see Azzopardi and Zuccon [8] for this extension). Another aspect that could be improved is the cost function. We have assumed that the cost of different actions are constant, yet they are often variable, and will change during the course of interaction (e.g., a query refinement may be less costly than expressing a new query or selecting from among several query suggestions). Also a more sophisticated and accurate cost model could be developed which may affect the model's predictions.

## 6 Discussion and Conclusions

In this chapter, we have described the process of building economic models and provided several examples in the context of information seeking and retrieval. In previous work [9, 10] we have also enumerated a number of other models that analyse other aspects of search interface components, e.g., when should facets be used, when is it better to issue a new query or is it better to take a query suggestion, how many results should we put on a result page query, and so on. While such models are relatively simple, they provide useful abstractions which focus the attention on the main levers that are likely to affect the behaviour of users. Furthermore, we are able to derive testable hypotheses about user behaviour. This is particularly useful because it provides a guide for experimentation which is grounded by theory. If the hypotheses are shown to hold, then the model provides a compact representation of the phenomena which designers and researchers can use when developing interface innovations or improving the underlying systems. For example, in the last scenario, if it is difficult to formulate an effective query, say in the context of image search, then we would expect that users would examine many more result items, and so we could adapt the system to show more results per page. Indeed, search engines provide ten blue links for web pages but hundreds of results for images. While useful and informative, there are, however, a number of challenges in taking the theory and putting it into practice.

The first major challenge concerns the estimation of the costs and benefits. Firstly, we have only considered the costs and benefits as common, but abstract units. However, if we wish to estimate the costs and benefits then we need to select some unit: this could be temporal, fiscal, physical or cognitive based. Often, though, time is used as a proxy for the cost. However, it would be more realistic to consider multiple cost functions for the different aspects of cost, and the trade-offs between them, i.e. a user might prefer to expand physical effort over cognitive effort. Or to combine the different costs functions into an overall cost function, where the different aspects are weighted according to their impact on the user's preferences. For example, Oulasvirta et al. [34] create a benefit function that is a linear combination of several criteria (usefulness, usability, value, etc.) in order to evaluate which features/actions an interface should afford users. In this case, rather than having one possible optimal solution, instead, depending on what aspect(s) are considered most important, different solutions arise. On the other

hand, what is the benefit that a user receives from their interactions with the system? Is it information, enjoyment, satisfaction, time, money? In our models we have made the assumption that the cost and benefit are in the same units, however, if we were to assume time as the cost, then the benefit would be how much time is saved (as done by Fuhr [20]). While this makes sense in the case of finding a name in a list, it does not make sense in all scenarios. For example, in the news search scenario, we could imagine that the amount of benefit is proportional to the new information found, and the benefit is relative to how helpful the information is in achieving their higher level work or leisure task. So, if we were to assume benefit as say, information gain (as done by Zhang and Zhai [51]), or user satisfaction (as done by Verma and Yilmaz [48]), then how do we express cost in the same unit? In this case a function is needed to map the benefits and costs into the same units (as done by Azzopardi and Zuccon [8]). Alternatively, the ratio between the benefit and the cost could be used instead as done in Information Foraging Theory (IFT) [38], or when performing a cost-effectiveness analysis. Once the units of measurement have been chosen, and instruments have been created to take such measurements, then the subsequent problem is how to accurately estimate the cost of the different interactions, and the benefit that is obtained from those interactions. This is very much an open problem.

A noted limitation of such models is the underlying assumption that people seek to maximise their benefit (e.g., the utility maximisation paradigm). This assumption has been subject to much scrutiny, and shown to break down in various circumstances leading to the development of behavioural economics. Kahneman and Tversky have shown that people are subject to various cognitive biases and that people often adopt heuristics which results in sub-optimal behaviours [26]. In their work on Prospect Theory, they argue that people have a more subjective interpretation of costs and benefits, and that people perceive and understand risk differently (i.e. some are more risk-averse than others). Whereas Simon argues that people are unlikely to be *maximisers* that relentlessly seek to maximise their benefit subject to a given cost [43], but rather *satisficers* who seek to obtain a satisfactory amount of benefit for the minimum cost. While the utility maximisation assumption is questionable, there is opportunity to extend these economics models presented here, and create more behavioural economic models that encode these more realistic assumptions about behaviour. As pointed out earlier though it is best to start simple and refine the models accordingly.

Another challenge that arises when developing such models is to ensure that there has been sufficient consideration of the user and the environment in which the interaction is taking place. In our models, we have largely ignored the cognitive constraints and limitations of users, nor have we explicitly modelled the environment. However, such factors are likely to influence behaviour. For example Oulasvirta et al. examined how choice overload (i.e. the paradox of choice) affects search behaviour and performance, finding that people were less satisfied when provided with more results [35]. While White showed that searchers would often seek confirmation of their *a priori* beliefs (i.e. confirmation bias), and were

again less satisfied with the results that contradicted them [49]. However within the Adaptive Interaction Framework [37] it is argued that the strategies that people employ are shaped by the adaptive, ecological and bounded nature of human behaviour. And as such, these biases and limitations should be taken into account when developing models of interaction. That is, by using the economic modelling approach presented above it is possible to develop models that maximize utility subject to such constraints. Essentially, the economic models here could be extended to incorporate such constraints (and thus assume Bounded Rationality [21, 43], for example). Furthermore, they could be incorporated into approaches such as Rational Analysis [2] or the Adaptive Interaction Framework [37], whereby a model includes user and environmental factors as well. Imposing such constraints, not only makes the models more realistic, but they are likely to provide better explanations of behaviour and thus better inform how we design interfaces and systems.

On a pragmatic point, the design and construction of experiments that specifically test the models can also be challenging. In the models we have described above, we used a technique called comparative statics, to consider what would happen to behaviour, when one variable is changed e.g., as cost goes up, less queries are issued. This required the assumption that all other variables were held constant. In practice, however, the manipulation of one variable, will invariably, influences other variables. For example, in the experiments performed examining the query cost hypothesis, one of the conditions contained query suggestions – the idea being that clicking on suggestions would be cheaper than typing in suggestions [7]. However, this inadvertently led to an increase in the amount of time on the search result page for this condition, which was attributed to the time spent reading through the suggestions [7]. However, this cost was not considered in the initial economic model proposed by Azzopardi [5]. This led to the revise model [6], described above, which explicitly models the cost of interacting with the search result page as well as the cost of interacting with snippets. These changes subsequently led to predictions that were consistent with the observed data. This example highlights the iterative nature of modelling and how refinements are often needed to create higher fidelity models.

To sum up, in this chapter, we have presented a tutorial for developing economic models of interaction. While we have presented several examples based on information seeking and retrieval, the same techniques can be applied to other tasks, interfaces and applications – in particularly where there is a trade-off between the cost and benefits. By creating such models, we can reason about how changes to the system will impact upon user behaviour before even implementing the said system. We can identify what variables are going to have the biggest impact on user behaviour – and focus our attention on addressing those aspects – thus guiding the experiments that we perform and the designs that we propose. Once a model has been developed and validated, then it provides a compact representation of the body of knowledge, so that others can use and extend the model developed. While we have noted above a number of challenges

in working with such models, the advantages are appealing and ultimately such models provide theoretical rigour to our largely experimental discipline.

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